



## Cambridge International AS & A Level

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**MATHEMATICS**

**9709/12**

Paper 1 Pure Mathematics 1

**May/June 2021**

**1 hour 50 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages. Any blank pages are indicated.

- 1 (a) Express  $16x^2 - 24x + 10$  in the form  $(4x + a)^2 + b$ . [2]

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- (b) It is given that the equation  $16x^2 - 24x + 10 = k$ , where  $k$  is a constant, has exactly one root.

Find the value of this root. [2]

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- 2 (a) The graph of  $y = f(x)$  is transformed to the graph of  $y = 2f(x - 1)$ .

Describe fully the two single transformations which have been combined to give the resulting transformation. [3]

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- (b) The curve  $y = \sin 2x - 5x$  is reflected in the y-axis and then stretched by scale factor  $\frac{1}{3}$  in the x-direction.

Write down the equation of the transformed curve. [2]

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- 3 The equation of a curve is  $y = (x - 3)\sqrt{x + 1} + 3$ . The following points lie on the curve. Non-exact values are rounded to 4 decimal places.

$$A(2, k) \quad B(2.9, 2.8025) \quad C(2.99, 2.9800) \quad D(2.999, 2.9980) \quad E(3, 3)$$

- (a) Find  $k$ , giving your answer correct to 4 decimal places. [1]

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- (b) Find the gradient of  $AE$ , giving your answer correct to 4 decimal places. [1]

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The gradients of  $BE$ ,  $CE$  and  $DE$ , rounded to 4 decimal places, are 1.9748, 1.9975 and 1.9997 respectively.

- (c) State, giving a reason for your answer, what the values of the four gradients suggest about the gradient of the curve at the point  $E$ . [2]

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- (c) Find  $\frac{d^2y}{dx^2}$ . [2]

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- (d) Determine the nature of the stationary point at  $(2, -3.5)$ . [2]

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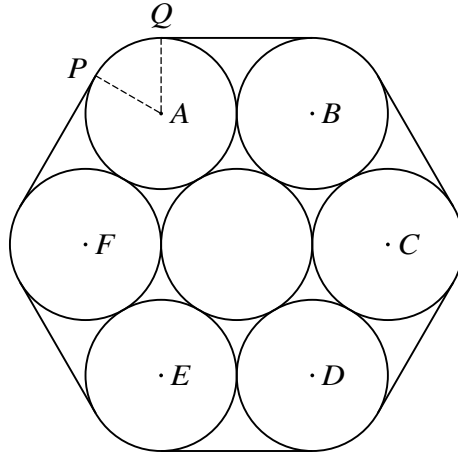
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The diagram shows a cross-section of seven cylindrical pipes, each of radius 20 cm, held together by a thin rope which is wrapped tightly around the pipes. The centres of the six outer pipes are  $A$ ,  $B$ ,  $C$ ,  $D$ ,  $E$  and  $F$ . Points  $P$  and  $Q$  are situated where straight sections of the rope meet the pipe with centre  $A$ .

- (a) Show that angle  $PAQ = \frac{1}{3}\pi$  radians. [2]

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- (b) Find the length of the rope. [4]

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(c) Find the area of the hexagon  $ABCDEF$ , giving your answer in terms of  $\sqrt{3}$ . [2]

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(d) Find the area of the complete region enclosed by the rope. [3]

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